

# Conical Similarity of Shock/Boundary-Layer Interactions Generated by Swept and Unswept Fins

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A parametric experimental investigation has been made of the class of three-dimensional shock wave/turbulent boundary-layer interactions generated by swept and unswept leading-edge fins. The fin sweepback angles were 0-65 deg at 5, 9, and 15 deg angles of attack. Two equilibrium two-dimensional turbulent boundary layers with a freestream Mach number of 2.95 and a Reynolds number of  $6.3 \times 10^7/\text{m}$  were used as incoming flow conditions. All of the resulting interactions were found to possess conical symmetry of the surface flow patterns and pressures outside of an initial inception zone. Further, these interactions were found to obey a simple conical similarity rule based on inviscid shock wave strength irrespective of fin sweepback or angle of attack. This is one of the first demonstrations of similarity among three-dimensional interactions produced by geometrically dissimilar shock generators.

## Nomenclature

$a$	= exponent in Reynolds number scaling law
$h$	= fin height, cm
$L_i$	= length along inviscid shock wave trace on test surface for the inception of conical flow, cm
$L_S$	= length along inviscid shock wave trace from fin leading edge, cm
$Lu_N$	= upstream influence length normal to inviscid shock wave trace on test surface, cm
$M_\infty$	= freestream Mach number
$M_N$	= $M_\infty \sin \beta_0$ , component of freestream Mach number normal to inviscid shock wave trace on test surface
$p$	= surface static pressure, N/m <sup>2</sup>
$p_\infty$	= static pressure of the incoming freestream flow, N/m <sup>2</sup>
$Re\delta$	= Reynolds number based on boundary-layer thickness
$x, y, z$	= Cartesian coordinate system (see Fig. 1)
$x_S$	= $x - z \cot \beta_0$ , streamwise coordinate measured from inviscid shock wave trace on test surface
$\alpha$	= fin angle of attack, deg
$\beta_0$	= inviscid shock wave angle on test surface measured from $x$ axis, deg
$\beta_A$	= angle between conical flow attachment line and $x$ axis, deg
$\beta_{S1}$	= angle between conical primary separation line and $x$ axis, deg
$\beta_{S2}$	= angle between conical secondary separation line and $x$ axis, deg
$\beta_U$	= angle between conical upstream influence line and $x$ axis, deg
$\delta$	= boundary-layer thickness, cm
$\delta_L$	= local boundary-layer thickness just ahead of the upstream influence line, cm
$\Delta L_S$	= displacement along the shock line of virtual conical origin from fin leading edge, cm
$\Delta z$	= spanwise displacement of virtual conical origin from fin leading edge, cm

$\lambda$	= fin leading-edge sweepback angle, deg
$\mu_\infty$	= freestream Mach angle, deg (= 19.8 deg at $M = 2.95$ )

## Introduction

THE interactions of shock waves and turbulent boundary layers constitute a classical problem of fluid dynamics that remains generally unsolved. These interactions, both two- and three-dimensional (2D and 3D), involve such a maze of flow regimes and peculiarities that no approximate analysis has shown much generality in their prediction. Further, numerical solutions of the nonlinear governing equations are currently possible only with limited methods of turbulence closure. This situation has led several investigators, including the present authors, to seek insight from experiments.

At least for 2D interactions, this experimental approach has been quite productive.<sup>1-3</sup> However, attempts to investigate 3D interactions have been fewer and less conclusive. Little overall understanding of the range of 3D interactions has been available until quite recently.

In an attempt to contribute to this poorly understood field, a series of parametric experiments has been performed in the past few years.<sup>4-12</sup> This paper presents recent results from that effort on the 3D interactions of turbulent boundary layers with shock waves generated by sharp fins.

Of many possible shock waves generators, the sharp fin has been used most often in 3D interaction experiments.<sup>4,5,7,12-30</sup> It produces a planar swept normal shock wave (also called a skewed or glancing oblique shock) with respect to a 2D boundary layer when its leading edge is normal to the plane of the boundary layer. This inviscid shock configuration, being planar, is perhaps the simplest 3D case available. However, the resulting 3D interaction of the shock with a viscous boundary layer is far from simple.

Even though this 3D interaction has been studied repeatedly, some investigators have failed to agree on basic considerations. For example, the literature<sup>4,5,7,12-27</sup> does not clarify whether the interaction is asymptotically cylindrical or conical in nature. Since sharp unbounded bodies naturally produce conical fields in supersonic flow, it appears likely to the present authors that earlier observations of quasicylindrical fin interactions were unintentionally contaminated by limited test channel or generator dimensions. In any case, there is still a need for a much improved understanding of fin-generated 3D shock/boundary-layer interactions.

The present study was made with that goal in mind. In particular, the parametric variation of a sharp fin leading-

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for unswept fins ( $\lambda=0^\circ$  deg), where it is planar and calculable from oblique shock theory. Otherwise, for  $\lambda>0$  deg but less than the detachment value, the shock forms a conical envelope exactly like that about a planar delta wing at angle of attack,<sup>35</sup> with the flat plate of Fig. 1 acting as a stream-wise plane of symmetry through the wing apex.

For present purposes, it is primarily necessary to know the intersection or "trace" of the inviscid shock on the flat plate. This trace is the best available reference position from which to measure the extent of the shock/boundary-layer interaction.<sup>11</sup> Observe that continuity requires the inviscid shock to be locally normal to the flat plate in Fig. 1 (a matter of considerable importance in the later discussion). Also observe that, according to conical flow theory, the inviscid shock trace on the plate must be a straight line through the coordinate origin in Fig. 1. The definition of this trace thus requires only that a single angle,  $\beta_0$ , be specified.

This angle can be estimated by an approximate method due to Roe,<sup>36</sup> calculated using a shock-fitting numerical solution of the Euler equations, or determined directly from experiments. The latter method was chosen as the most accurate and straightforward for present purposes. Flat delta wings duplicating the  $(\alpha,\lambda)$  parameters of the present fin shock generators were mounted on the wind tunnel centerline and observed by shadowgraph visualization. As illustrated in Fig. 3, this allowed the direct measurement of  $\beta_0$  from shadowgrams.

Further, for delta wings with shocks attached to the leading edges, serrations on these leading edges generated Mach waves on the conical shock envelope from which the shock shape could be determined. An example of this is given in Fig. 4. The resulting shock shapes and  $\beta_0$  values

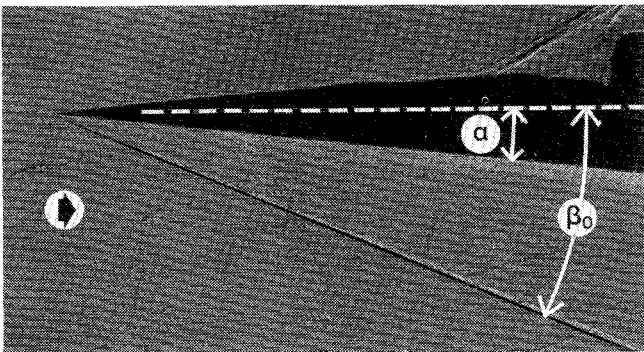


Fig. 3 Shadowgram of shock wave produced by  $\alpha=5$  deg,  $\lambda=55$  deg delta wing.

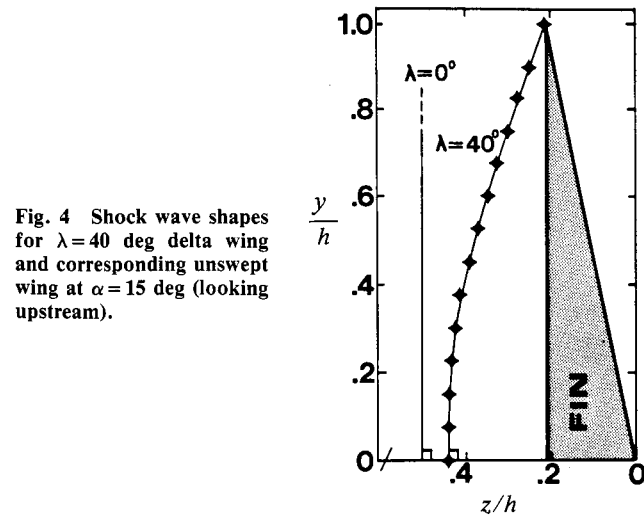


Fig. 4 Shock wave shapes for  $\lambda=40$  deg delta wing and corresponding unswept wing at  $\alpha=15$  deg (looking upstream).

were in general agreement with calculated values using Roe's method,<sup>36</sup> although the latter tended to underestimate the measured values of  $\beta_0$  somewhat.

A summary of the shadowgram results for  $\beta_0(\alpha,\lambda)$  is plotted in Fig. 5. Clearly,  $\beta_0$  is a strong function of  $\alpha$  but a mild function of  $\lambda$ . These data are prerequisites for the following analysis of fin-generated conical shock/boundary-layer interactions.

Conical Interaction Symmetry

Figure 6a presents an example of a kerosene/lamp-black/adhesive tape surface flow visualization pattern show-

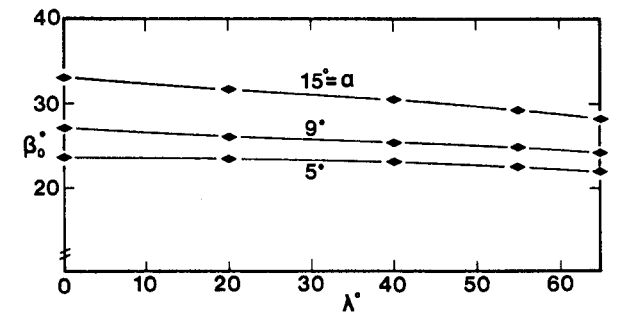


Fig. 5 Measured and interpolated shock angles  $\beta_0$  for  $M_\infty=2.95$ .

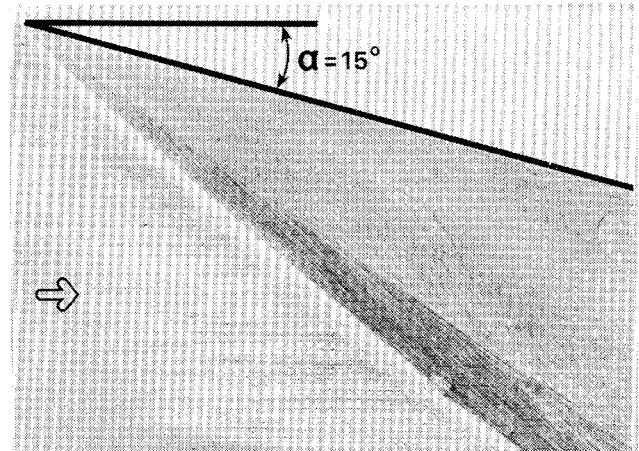


Fig. 6a Example of kerosene/lampblack/adhesive tape surface-flow streak pattern for  $\alpha=15$  deg,  $\lambda=0$  deg fin interaction on flat plate.

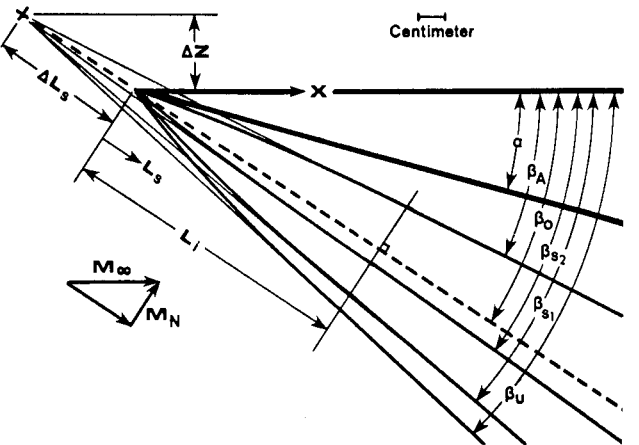


Fig. 6b Corresponding diagram of interaction footprint features and notation.

ing the "footprint" of the  $\alpha=15$  deg,  $\lambda=0$  deg fin interaction. Figure 6 is a geometrically similar diagram of this footprint showing the framework and defining the parameters used in the present analysis of such patterns. Distances are represented either by the streamwise  $x$  coordinate or by the  $L_S$  coordinate. All angles are measured from the  $x$  axis.

For every  $(\alpha, \lambda)$  combination tested, the interaction footprint was observed to begin at the flat-plate/fin leading-edge junction with a curved, nonconical "inception zone."<sup>11,25</sup> Beyond this zone, i.e., for  $L_S > L_i$ , conical interaction symmetry was observed.<sup>11,12,24,25,27-30,37</sup>

By definition, all surface features in the conical region are bounded by rays from a common origin. However, due to the inception zone this origin does not coincide with the plate/leading-edge junction. It is instead a virtual origin that is displaced by a distance  $\Delta L_S$  along the inviscid shock line, as shown in Fig. 6b.

Four features of the surface streak pattern of Fig. 6a are indicated in Fig. 6b. These features run asymptotically into straight lines through the virtual conical origin at angles  $\beta_{ij}$  with the  $x$  axis. They are the upstream influence line  $\beta_U$ , the primary separation line at  $\beta_{S1}$ , the secondary separation line at  $\beta_{S2}$ , and the primary reattachment line at  $\beta_A$ . Also shown for reference is the inviscid shock trace (dashed line) at  $\beta_0$ , although it does not constitute a surface pattern feature.

Obviously, some of these features are present in the surface streak patterns only when the shock is strong enough to cause 3D separation of the boundary layer. Also, note that the fin/plate junction at angle  $\alpha$  in Fig. 6b does not lie along a ray from the conical virtual origin and thus is not a conical feature of the interaction. (Indeed, a close examination of the surface patterns reveals flow across this junction.)

Asymptotically conical symmetry was observed for all the present fin interactions in both surface-streak patterns and surface pressure distributions. This is shown by the example of the  $\alpha=15$  deg,  $\lambda=55$  deg fin interaction in Fig. 7. The normalized surface pressure  $p/p_\infty$  is plotted against  $x_S/(z+\Delta z)$  and is shown to be invariant with spanwise distance in these coordinates.<sup>‡</sup> Thus, the fact that the streamwise interaction scale is proportional to the spanwise distance from the virtual origin in Fig. 7 and in the other pressure distributions (not shown) lends further support to conical interaction symmetry.

#### Conical Interaction Similarity

Having observed conical symmetry for both swept and unswept fin interactions raises the possibility of similarity among them. In other words, are swept and unswept interactions fundamentally different or are they similar in some appropriate framework? This question is addressed by the results shown in Fig. 8.

The ordinate of Fig. 8 represents an "interaction response function," i.e., the difference between any of the conical surface feature angles  $\beta_{ij}$  and the shock angle  $\beta_0$ . The abscissa of Fig. 8 represents the shock wave strength at the test surface by the quantity  $\beta_0 - \mu_\infty$ . The results show clearly that the interaction features are functions of  $\beta_0 - \mu_\infty$  (or of  $\beta_0$  alone, since  $\mu_\infty = \text{const}$ ) irrespective of the fin geometry parameters  $\alpha$  and  $\lambda$ .

This discovery amounts to a straightforward conical similarity of fin-generated 3D interactions. The fin geometry and overall shock shape appear not to influence the shock/boundary-layer interaction other than in specifying the inviscid shock angle at the test surface. The authors believe this to be a unique demonstration of similarity

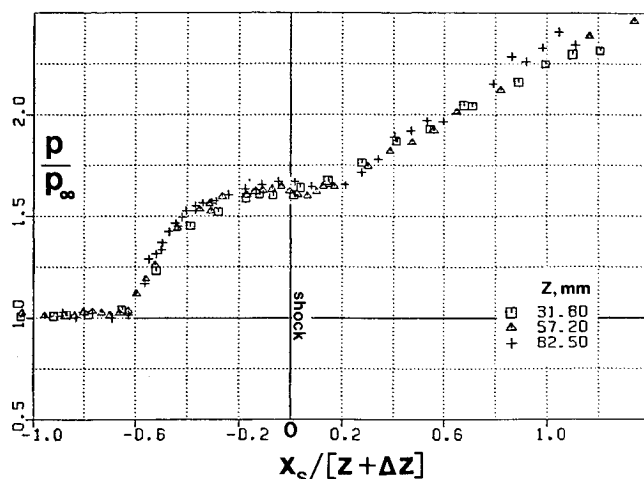


Fig. 7 Streamwise surface pressure distributions for  $\alpha=15$  deg,  $\lambda=55$  deg swept fin interaction, scaled by spanwise distance from virtual conical origin.

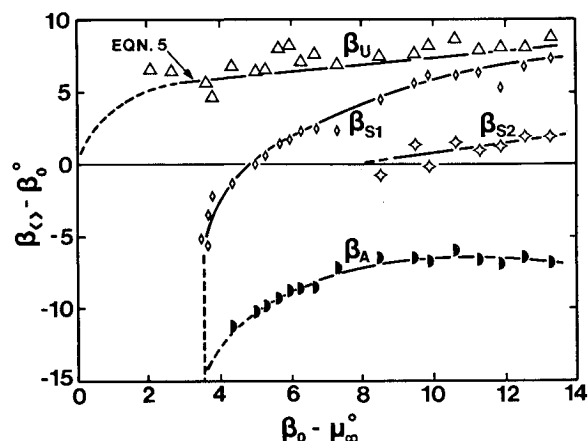


Fig. 8 Angular response of interaction features vs shock wave strength, demonstrating results of parametric variation of  $\alpha$  and  $\lambda$ .

among interactions produced by geometrically dissimilar shock generators.

The following physical explanation is put forth for this phenomenon. Recall that continuity requires the inviscid shock to be normal to the test surface in all cases. If the inviscid shock configuration in the immediate vicinity of the boundary layer it interacts with is of primary importance in specifying the interaction, then planar and weakly curved shocks of equal  $\beta_0$  will produce equivalent interactions. The overall shock shape will be immaterial in this case<sup>§</sup> and the conical similarity shown in Fig. 8 will then be a direct result.

This explanation of conical similarity assumes that the 3D interaction problem can be simplified to local rather than global flow conditions. The general validity of this assumption for other than fin-generated interactions with both separation and reattachment in the plane of the incoming boundary layer is a subject of ongoing study.<sup>12</sup>

A second assumption is also implicit in the above physical explanation. While the character of the flows observed here

<sup>‡</sup>The use of  $(x, z)$  rather than shock-based normal and tangential coordinates here is admittedly clumsy, but necessary since the surface pressure tap rows were all parallel to the  $x$  axis. Note further that the  $\Delta z$  value used in constructing Fig. 7 was obtained from the corresponding surface-streak pattern, as was the case for all the present experiments.<sup>28</sup>

<sup>§</sup>Recent research<sup>12</sup> has shown that, for interactions due to different shock generators where the inviscid shock wave radius of curvature is comparable to the boundary-layer thickness, the shock shape must also be taken into account along with the angle  $\beta_0$ . For all the present fin interactions, however, the shock radius was at least an order of magnitude larger than the boundary-layer thickness.

is clearly the result of an interaction of viscous and inviscid phenomena, the latter appear to play a predominant role in specifying the overall flow symmetry and scaling parameters.

A further test of conical similarity should be made by varying  $M_\infty$ . While  $\beta_0$  alone is sufficient to specify the shock strength with  $M_\infty$  fixed, note that  $M_N = M_\infty \sin \beta_0$  is required for that purpose when  $M_\infty$  varies. Whether or not conical similarity based on  $M_N$  holds in general should be one subject of future study.

Finally, before leaving Fig. 8, there are several additional observations of value:

1) Incipient primary flow separation occurs at  $\beta_0 - \mu_\infty = 3.5$  deg, corresponding closely to Korkegi's<sup>38</sup> simple criterion.

2) Incipient "secondary separation" occurs at  $\beta_0 - \mu_\infty = 8$  deg, corresponding closely to Zheltovodov's<sup>24</sup> modification of Korkegi's criterion.

3) Stanbrook's<sup>14</sup> definition of incipient 3D separation as the condition where the surface-streak angle first equals the shock angle is not supported by Fig. 8. In fact, incipient separation occurs when the streak angle is about 6 deg less than the shock angle in the present experiments.

4) The angular difference between the upstream influence and primary separation lines is a significant fraction of the total interaction footprint near incipient separation, but shrinks toward a negligible value as the shock strength is increased.

5) Finally, note that the region of vanishingly weak shock strength in Fig. 8 [ $0 \leq (\beta_0 - \mu_\infty) \leq 4$  deg] apparently involves a rapid nonlinear growth of upstream influence. This was first noted by Dolling,<sup>7</sup> who also pointed out that accurate measurements in this weak shock region are prohibitively difficult.

#### Reynolds Number and Shock Strength Similarity

Settles<sup>8</sup> has previously formulated a scaling law for Reynolds number effects on 3D interactions that succeeded in correlating the results of both swept compression corner<sup>8,39</sup> and unswept fin<sup>7,29,30</sup> interactions. Dolling<sup>7</sup> extended this scaling law to include variable shock strength in unswept fin interactions by way of the normal Mach number  $M_N$ . In coordinates normal and tangential to the inviscid shock

wave, this scaling law can be written for the upstream influence as

$$(Lu_N/\delta_L)(Re\delta_L^a/M_N) = f[(L_S/\delta_L)Re\delta_L^a] \quad (1)$$

where  $a$  has an empirical value of about  $1/3$  when  $M_\infty = 2.95$ .

The applicability of Eq. (1) to both swept and unswept fin interactions has been tested by plotting the present upstream influence data in terms of the above coordinates in Fig. 9. Included in this figure are 41 upstream influence lines embodying parametric variations of  $\alpha$ ,  $\lambda$ ,  $\delta_L$ , and  $Re\delta_L$ . The result clearly indicates that Eq. (1) is applicable to both swept and unswept fin interactions within the present ranges of parameters.

One observation drawn from Fig. 9 is that the simple normalization of  $Lu_N$  by  $M_N$  effectively correlates variations in shock strength due to both  $\alpha$  and  $\lambda$  variations of the fin geometry. This result is thus an additional confirmation of the conical similarity principle, since

$$M_N = M_N(M_\infty, \alpha, \lambda) = M_\infty \sin \beta_0(\alpha, \lambda) \quad (2)$$

As stated earlier, a more rigorous test would be possible if data were available at other values of  $M_\infty$ . Simple normalization by  $M_N$  could be an oversimplification with a limited range of validity, although it is certainly effective for the present limited range of fin interactions at  $M_\infty \approx 3$  as supported by Fig. 9. However, recent research<sup>12</sup> has shown that related interactions, produced by swept compression corners at the same  $M_\infty$ , scale according to  $M_N^2$  rather than  $M_N$ . This raises questions that cannot be answered at present, other than to point out that  $M_N^2$  scaling has the physical justification of being directly related to the shock wave strength via the pressure ratio, while simple  $M_N$  scaling apparently lacks any such justification.

Returning to Fig. 9, note that the length of the nonconical interaction inception zone  $L_i$  is given approximately by

$$(L_i/\delta_L)Re\delta_L^{1/3} \sim 1600 \quad (M_\infty = 2.95) \quad (3)$$

This number is difficult to determine accurately due to the asymptotic joining of the inception and conical zones. Further, recent research<sup>40</sup> covering larger values of  $\alpha$  indicates a tendency for  $L_i$  to grow as  $\alpha$  increases.

One consequence of Eq. (3) is that the inception zone for the case of an extremely thin boundary layer and high Reynolds number may have a negligible dimensional length, as found by Zubin and Ostapenko.<sup>25</sup> On the other hand, the opposite conditions can expand the length of the inception zone beyond the size of the test facility itself (as seen in the results of Token,<sup>18</sup> even though his experiments were carried out on a massive dimensional scale).

Clearly, the inception zone, which is the only dimensional region in an otherwise nondimensional conical interaction, can itself be understood only in nondimensional terms. A rational hypothesis for its existence<sup>41</sup> is based on the comparable scales of the incoming boundary layer and the initial interaction region near the fin leading-edge/flat-plate junction, hence the  $Re\delta_L$  dependence in Eq. (3).

Outside the inception zone the flow has been shown to be conical, so length dimensions and Reynolds number no longer have any relevance to the scaling. In this case, Eq. (1) may be rewritten as

$$Lu_N/(L_S + \Delta L_S) = \tan(\beta_0 - \beta_0) = c_I M_N \quad (L_S \geq L_i) \quad (4)$$

where the coordinate origin has been shifted to the virtual conical origin and the constant  $c_I \approx 0.09$  is simply the slope

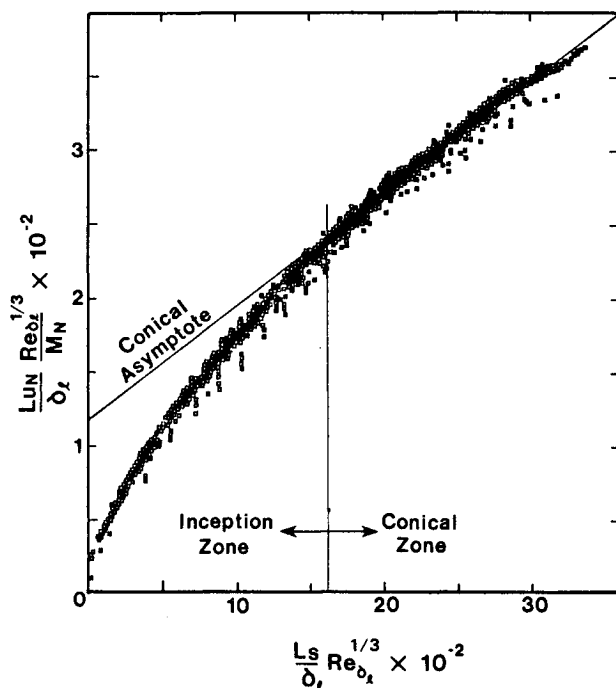


Fig. 9 Scaling of upstream influence lines across the present  $(\alpha, \lambda)$  range in nondimensional form.

of the conical asymptote in Fig. 9. Expanding  $M_N$ ,

$$\tan(\beta_U - \beta_0) = c_1 M_\infty \sin \beta_0 = c_2 \sin \beta_0 \quad (M_\infty = 2.95)$$

$$(\beta_U - \beta_0) = \arctan(0.26 \sin \beta_0) \quad (5)$$

where  $c_2 = c_1 M_\infty = 0.26$ . Equation (5) is, in fact, the straight line through the  $\beta_U$  data shown in Fig. 8. Thus, at least for the upstream influence, the normal Mach number scaling of Eq. (1) and the principle of conical similarity are equivalent over the range of the present experiments.

### Conclusion

A parametric experimental study of swept-fin-induced three-dimensional shock wave/turbulent boundary-layer interactions has been carried out at  $M_\infty = 2.95$ . Included in the study were 2 incoming boundary layers, 2 values of Reynolds number, and 24 values of fin sweepback and angle of attack. The results consisted of surface and flowfield visualization data and surface pressure measurements. A scaling framework was developed for the analysis of these results. The major conclusions drawn from this analysis are:

- 1) Three-dimensional boundary-layer separation was clearly observed at lines of streak convergence on the interaction test surface.
- 2) Asymptotically conical shock/boundary-layer interactions were produced under all the present test conditions.
- 3) These interactions were found to obey a conical similarity principle based on local shock wave strength in the vicinity of the boundary layer irrespective of fin sweepback or angle of attack.
- 4) Scaling laws for Reynolds number and normal Mach number effects, developed in earlier studies, were found to apply equally well to the present swept and unswept fin interactions.

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